



- Answer all the following questions
- Illustrate your answers with sketches when necessary.
- The exam consists of two pages

- No. of questions: 5
- Total marks: 80
- Examiner: Dr. Ibtesam Omer

Question 1 [20 Marks]

(a) Given $h_{ie} = 2.4 \text{ k}\Omega$, $h_{fe} = 100$, $h_{re} = 4 \times 10^{-4}$ and $h_{oe} = 25 \mu\text{S}$, sketch the:

Ans:

(i) Common-emitter **hybrid** equivalent model.

$$h_{ie} = \beta r_e = 2.4 \text{ k}\Omega$$

$$h_{fe} = \beta = 100$$

$$h_{re} = 4 \times 10^{-4}$$

$$h_{oe} = 25 \mu\text{S}$$

(ii) Common-emitter **r_e** equivalent model.

$$r_e = 2.4 \text{ k}\Omega / 100 = 24 \Omega$$

$$r_o = 1 / h_{oe} = 1 / 25 \mu\text{S} = 40 \text{ k}\Omega$$

(b) For the common-base configuration of Figure 1, the emitter current is 3.2 mA and α is 0.99.

If the applied voltage is 48 mV and the load is 2.2 k Ω

Determine the following:

- r_e
- Z_i
- I_c
- V_o
- A_v
- I_b

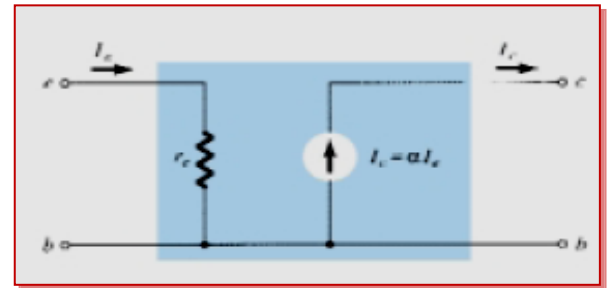
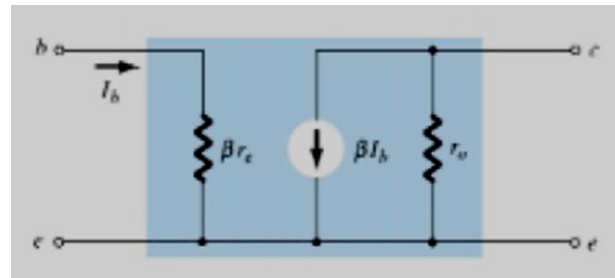
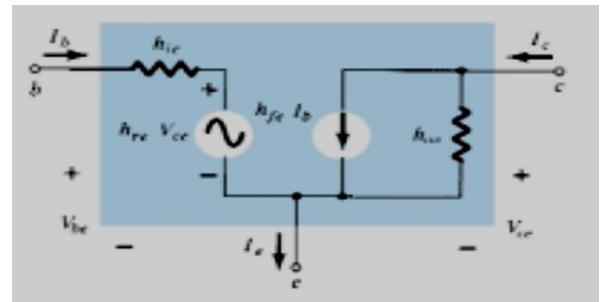


Figure (1) Common-base r_e equivalent circuit

Ans:

$$(a) r_e = \frac{V_i}{I_i} = \frac{48 \text{ mV}}{3.2 \text{ mA}} = 15 \Omega$$

$$(b) Z_i = r_e = 15 \Omega$$

$$(c) I_c = \alpha I_e = (0.99)(3.2 \text{ mA}) = 3.168 \text{ mA}$$

$$(d) V_o = I_c R_L = (3.168 \text{ mA})(2.2 \text{ k}\Omega) = 6.97 \text{ V}$$

$$(e) A_v = \frac{V_o}{V_i} = \frac{6.97 \text{ V}}{48 \text{ mV}} = 145.21$$

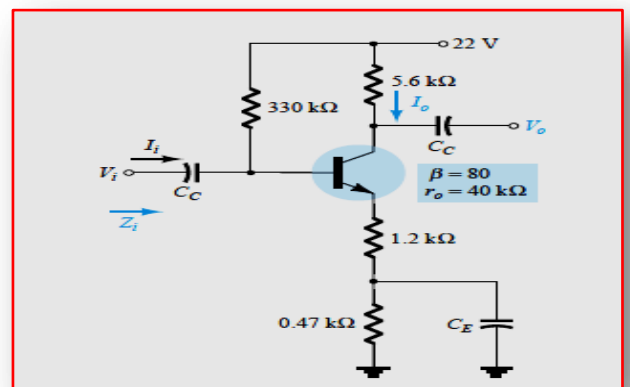
$$(f) I_b = (1 - \alpha) I_e = (1 - 0.99) I_e = (0.01)(3.2 \text{ mA}) = 32 \mu\text{A}$$

Question 2 [14 Marks]

(a) For the network of Figure 2 at $r_o = \infty \text{ k}\Omega$:

- Determine r_e .
- Find Z_i and Z_o .
- Calculate A_i and A_v .

Ans:



$$\begin{aligned}
 (a) \quad I_B &= \frac{V_{CC} - V_{BE}}{R_B + (\beta + 1)R_E} \\
 &= \frac{22V - 0.7V}{330k\Omega + (81)(1.2k\Omega + 0.47k\Omega)} = \frac{21.3V}{465.27k\Omega} \\
 &= 45.78\mu A
 \end{aligned}$$

$$I_E = (\beta + 1)I_B = (81)(45.78\mu A) = 3.71mA$$

$$r_e = \frac{26mV}{I_E} = \frac{26mV}{3.71mA} = 7\Omega$$

$$(b) \quad r_o < 10(R_C + R_E)$$

$$\therefore Z_b = \beta r_e + \left[\frac{(\beta + 1) + R_C/r_o}{1 + (R_C + R_E)/r_o} \right] R_E$$

$$= (80)(7\Omega) + \left[\frac{(81) + 5.6k\Omega/40k\Omega}{1 + 6.8k\Omega/40k\Omega} \right] 1.2k\Omega$$

$$= 560\Omega + \left[\frac{81 + 0.14}{1 + 0.17} \right] 1.2k\Omega$$

$$(\text{note that } (\beta + 1) = 81 \gg R_C/r_o = 0.14)$$

$$= 560\Omega + [81.14/1.17] 1.2k\Omega = 560\Omega + 83.22k\Omega$$

$$= 83.78k\Omega$$

$$Z_i = R_B \parallel Z_b = 330k\Omega \parallel 83.78k\Omega = 66.82k\Omega$$

$$A_v = -\frac{\beta R_C (1 + \frac{r_e}{r_o}) + \frac{R_C}{r_o}}{1 + \frac{R_C}{r_o}}$$

$$= -\frac{(80)(5.6k\Omega) \left(1 + \frac{7\Omega}{40k\Omega}\right) + \frac{5.6k\Omega}{40k\Omega}}{1 + 5.6k\Omega/40k\Omega}$$

$$= -\frac{(5.35) + 0.14}{1 + 0.14}$$

$$= -4.57$$

$$\begin{aligned}
 (c) \quad A_i &= -A_v \frac{Z_i}{R_C} = -(-4.57)(66.82k\Omega)/5.6k\Omega \\
 &= 54.53
 \end{aligned}$$

(b) What is the expected amplification of a BJT transistor amplifier if the dc supply is set to zero volts?

Ans:

If the dc supply is set to zero volts the amplification will be zero.

Question 3 [18 Marks]

(a) Determine the voltage gain, the power gain, and the efficiency of the **class A** power amplifier in figure 3. Assume $\beta_{ac(Q1)} = \beta_{ac(Q2)} = 200$ and $\beta_{ac(Q3)} = 50$. Express the power gain as a decibel power gain.

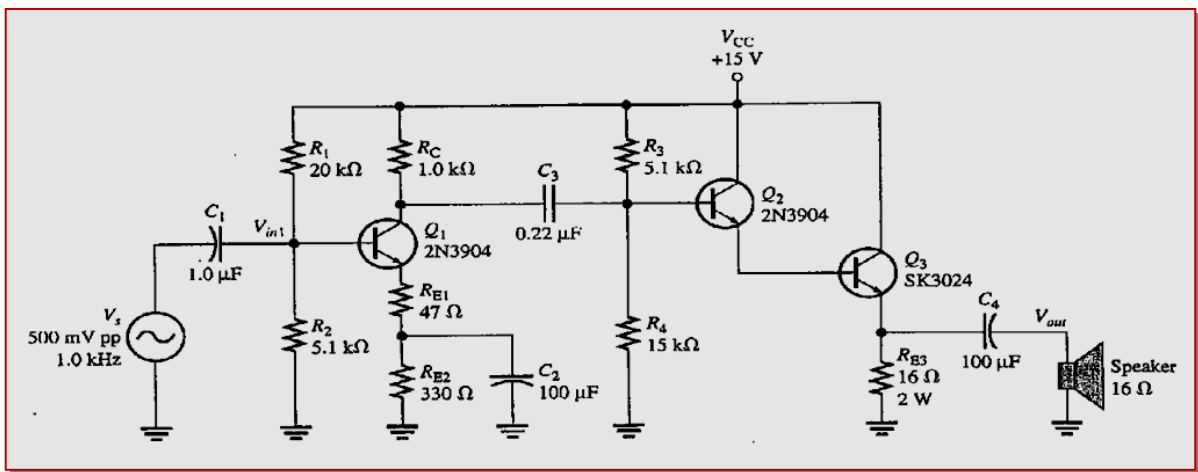


Figure (3) Class A Power Amplifier.

Ans:

$$A_{v(\text{tot})} = A_{v1} * A_{v2} * A_{v3}$$

A_{v2}, A_{v3} is emitter follower so $A_{v2} = A_{v3} = 1$

After Ac Analysis

From common emitter configuration $A_{v1} = (-R_{c1}) / (R_{E1} + r_{e(Q1)})$

First stage:

The ac collector resistance of the first stage is R_{c1} in parallel with the input resistance to the second stage.

$$\begin{aligned} R_{c1} &= R_C \parallel [R_3 \parallel R_4 \parallel \beta_{ac(Q2)} \beta_{ac(Q3)} (R_{E3} \parallel R_L)] \\ &= 1.0 \text{ k}\Omega \parallel [5.1 \text{ k}\Omega \parallel 15 \text{ k}\Omega \parallel (200)(50)(16 \Omega \parallel 16 \Omega)] \\ &= 1.0 \text{ k}\Omega \parallel (5.1 \text{ k}\Omega \parallel 15 \text{ k}\Omega \parallel 80 \text{ k}\Omega) = 1.0 \text{ k}\Omega \parallel 3.63 \text{ k}\Omega = 784 \Omega \end{aligned}$$

The voltage gain of the first stage is the ac collector resistance, R_{c1} , divided by the ac emitter resistance, which is the sum of $R_{E1} + r'_{e(Q1)}$. The approximate value of $r'_{e(Q1)}$ is determined by first finding I_E .

$$\begin{aligned} V_B &= \left(\frac{R_2 \parallel (\beta_{ac(Q1)}(R_{E1} + R_{E2}))}{R_1 + R_2 \parallel (\beta_{ac(Q1)}(R_{E1} + R_{E2}))} \right) V_{CC} \\ &= \left(\frac{5.1 \text{ k}\Omega \parallel 200(377 \Omega)}{20 \text{ k}\Omega + 5.1 \text{ k}\Omega \parallel 200(377 \Omega)} \right) 15 \text{ V} \\ &= \left(\frac{4.78 \text{ k}\Omega}{20 \text{ k}\Omega + 4.78 \text{ k}\Omega} \right) 15 \text{ V} = 2.89 \text{ V} \\ I_E &= \frac{V_B - 0.7 \text{ V}}{R_{E1} + R_{E2}} = \frac{2.89 \text{ V} - 0.7 \text{ V}}{377 \Omega} = 5.81 \text{ mA} \\ r'_{e(Q1)} &= \frac{25 \text{ mV}}{I_E} = \frac{25 \text{ mV}}{5.81 \text{ mA}} = 4.3 \Omega \end{aligned}$$

The voltage gain of the first stage with the loading of the second stage taken into account.

$$A_{v1} = -\frac{R_{c1}}{R_{E1} + r'_{e(Q1)}} = -\frac{784 \Omega}{47 \Omega + 4.3 \Omega} = -15.3$$

The negative sign is for inversion.

$$R_{in(\text{tot})} = R1 \parallel R2 \parallel \beta_{ac(Q1)} (r'_{e(Q1)} + R_{E1})$$

$$= 20 \text{ k}\Omega \parallel 5.1 \text{ k}\Omega \parallel 200(47 \Omega + 4.3 \Omega) = 2.9 \text{ k}\Omega$$

$$A_{v(\text{tot})} = A_{v1} * A_{v2} * A_{v3} = -15.3$$

$$A_p = (A_{v(\text{tot})})^2 (R_{in(\text{tot})} / R_L) = 42,429$$

$$\text{dB} = 10 \text{ Log } A_p = 10 \text{ Log } 42,429 = 46.23 \text{ dB}$$

(b) List the capacitances that affect high frequency gain in BJT amplifier. Explain why the coupling capacitors do not have a significant effect on gain at sufficiently high signal frequencies.

BJT: C_{be} , C_{bc} , and C_{ce}

Question 4 [12 Marks]

For the network shown in figure 4:

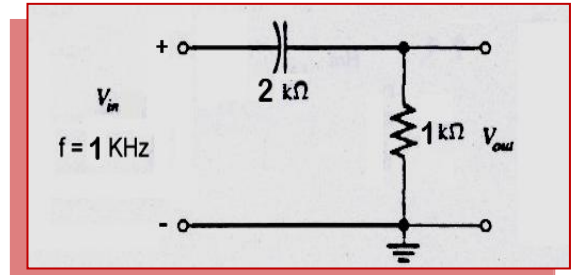


Figure (4) R-C combination that will define cut off frequency

- (a) Determine the corner frequency.
- (b) Determine the mathematical expression for the magnitude of the voltage gain.
- (c) Determine the mathematical expression for the angle by which V_o leads V_i .
- (d) Sketch the frequency response of θ .

Ans:

$$f_1 = \frac{1}{2\pi RC}$$

a)

$$X_c = 1/2\pi fC = 2k\Omega$$

$$C = 7.96 \times 10^{-8} \text{ farad}$$

$$f_1 = 1/2 \pi RC = 2 \text{ kHz}$$

b)

If the gain equation is written as

$$A_v = \frac{V_o}{V_i} = \frac{R}{R - jX_c} = \frac{1}{1 - j(X_c/R)} = \frac{1}{1 - j(1/\omega CR)} = \frac{1}{1 - j(1/2\pi fCR)}$$

and using the frequency defined above,

$$A_v = \frac{1}{1 - j(f_1/f)}$$

In the magnitude and phase form,

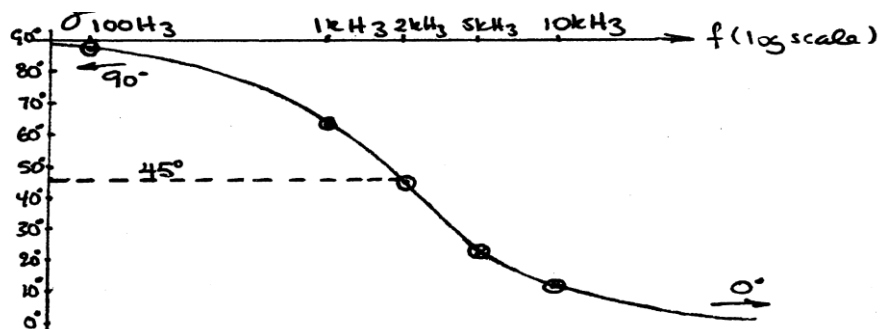
$$A_v = \frac{V_o}{V_i} = \underbrace{\frac{1}{\sqrt{1 + (f_1/f)^2}}}_{\text{magnitude of } A_v} \underbrace{\angle \tan^{-1}(f_1/f)}_{\text{phase } \angle \text{ by which } V_o \text{ leads } V_i}$$

c)

$$\theta = \tan^{-1} \frac{f_1}{f}$$

d)

- f=100 Hz $\theta=87.13^\circ$
- f=1 kHz $\theta=63.43^\circ$
- f=2 kHz $\theta=45^\circ$
- f=5 kHz $\theta=21.8^\circ$
- f=10 kHz $\theta=11.3^\circ$

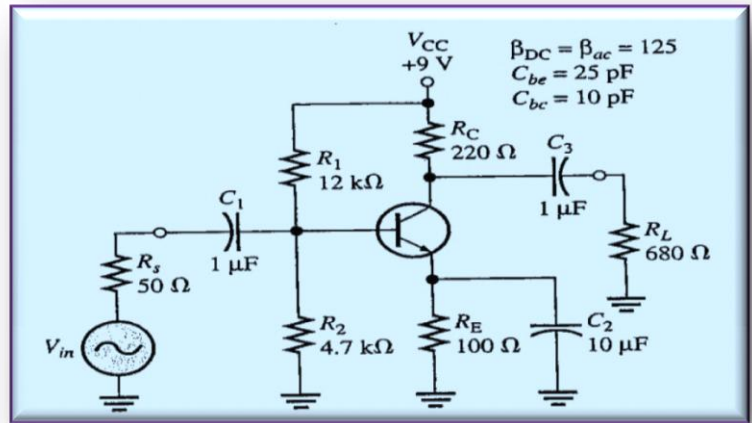


Question 5 [16 Marks]

For the BJT amplifier in figure 5:

(a) Determine the critical frequencies associated with the low frequency response.

(b) Which is the dominant critical frequency? Sketch the Bode Plot.



Ans:

(a) Figure (5) Loaded BJT amplifier with capacitors that affect the low-frequency response

$$R_{IN(base)} = \beta_{DC} R_E = 12.5 \text{ k}\Omega$$

$$V_E = \left(\frac{R_2 \parallel R_{IN(base)}}{R_1 + R_2 \parallel R_{IN(base)}} \right) 9 \text{ V} - 0.7 \text{ V} = \left(\frac{4.7 \text{ k}\Omega \parallel 12.5 \text{ k}\Omega}{12 \text{ k}\Omega + 4.7 \text{ k}\Omega \parallel 12.5 \text{ k}\Omega} \right) 9 \text{ V} - 0.7 \text{ V} = 1.3 \text{ V}$$

$$I_E = \frac{V_E}{R_E} = \frac{1.3 \text{ V}}{100 \Omega} = 13 \text{ mA}$$

$$r'_e = \frac{25 \text{ mV}}{13 \text{ mA}} = 1.92 \Omega$$

$$R_{in(base')} = \beta_{ac} r'_e = (125)(1.92 \Omega) = 240 \Omega$$

$$R_{in} = 50 \Omega + R_{in(base')} \parallel R_1 \parallel R_2 = 50 \Omega + 240 \Omega \parallel 12 \text{ k}\Omega \parallel 4.7 \text{ k}\Omega = 274 \Omega$$

For the input network:

$$f_c = \frac{1}{2\pi R_{in} C_1} = \frac{1}{2\pi (274 \Omega)(1 \mu\text{F})} = 578 \text{ Hz}$$

For the output network:

$$f_c = \frac{1}{2\pi (R_C + R_L) C_3} = \frac{1}{2\pi (900 \Omega)(1 \mu\text{F})} = 177 \text{ Hz}$$

For the bypass network:

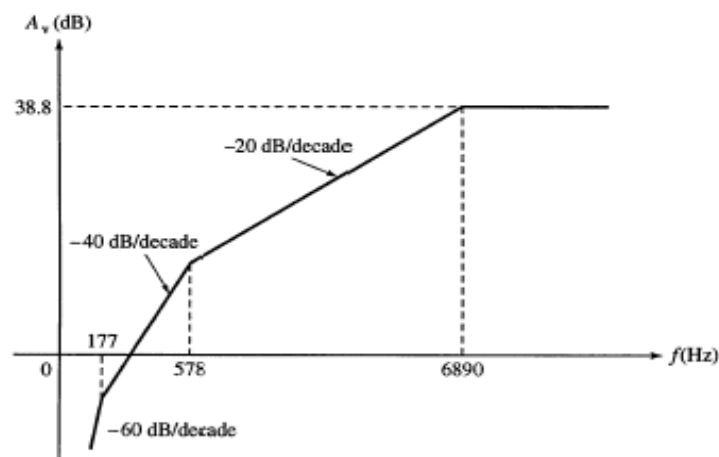
$$R_{TH} = R_1 \parallel R_2 \parallel R_s = 12 \text{ k}\Omega \parallel 4.7 \text{ k}\Omega \parallel 50 \Omega \cong 49.3 \Omega$$

$$f_c = \frac{1}{2\pi (r'_e + R_{TH} / \beta_{DC} \parallel R_E) C_2} = \frac{1}{2\pi (2.31 \Omega)(10 \mu\text{F})} = 6.89 \text{ kHz}$$

$$A_v = \frac{R_C \parallel R_L}{r'_e} = \frac{220 \Omega \parallel 680 \Omega}{1.92 \Omega} = 86.6$$

$$A_v(\text{dB}) = 20 \log(86.6) = 38.8 \text{ dB}$$

(b) The bypass network produces the dominant critical frequency. See the following figure



Good luck
Dr. Abtesam Omer